

Discussion of  
Taxation, Redistribution and Frictional Labor  
Supply  
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# Introduction

- ▶ This paper considers optimal taxation when workers differ not only in skills, but job matching luck.
- ▶ Argues that with reasonable parameters, linear taxes should be lower than if workers did not face matching luck.
- ▶ Very neat idea. I'm a bit skeptical regarding whether the lower taxes come from general equilibrium effects. I'll focus on that later.

## Basic Idea

- ▶ Put together Burdett and Mortensen model with a Mirrlees *environment* (people of differing skill produce output) and do a Ramsey like optimal tax exercise.
- ▶ Burdett and Mortensen: Walmart vs. Costco. Walmart doesn't pay as much and churns through workers. Costco pays a lot and keeps its workers for a long time.
- ▶ Burdett and Mortensen build model where this happens in equilibrium. Key thing is on-the-job search. Walmart workers get random opportunities to trade up to Costco, which they grab.
- ▶ So firms trade off gains of paying low wages with loss of having your job filled less of the time.

## Their model

- ▶ As usual for a Mirrlees model, agents have different skills  $\theta$ . If they work  $\ell$  hours, they produce  $y = \theta\ell$  units of output.
- ▶ But a twist is that what I will call *land* (and they call firms) is a necessary input to production.
- ▶ Workers need to be matched to land to produce.
- ▶ Unmatched workers are unemployed. They get Poisson shocks to match them with landowners who post rent prices. They take whatever land gives them a deal better than being unmatched.
- ▶ Matched workers also get Poisson matching shocks. Move to lower rent land whenever possible.

# Policy

- ▶ Most of paper deals with Ramsey affine taxation. (As opposed to introducing incentive constraints a la Mirrlees.)
- ▶  $c = \textit{benefit} + (1 - \tau)\textit{output} - \textit{rent}$ .
- ▶ Complicated equilibrium steady state distribution of consumption, outputs, and rents all as functions of  $\theta$  types.
- ▶ (Nice bit of modeling to pull this off.)
- ▶ Authors derive expressions showing this effect and that effect with new terms.

## My Contribution

- ▶ Why the lower taxes?
- ▶ I would have thought with an added source of consumption inequality and given a redistribution loving objective function, that would lead to higher, not lower taxes.
- ▶ So my contribution is to try to figure out what is going on.
- ▶ (if I'm wrong, BFI still has to pay for my expenses.)

## My Contribution

- ▶ My strategy: Come up with simple *static* optimal tax problem where several things which should be determined in equilibrium are just made by me into fixed parameters.
  - ▶ Fraction of unemployed. (I think this is in steady state directly pinned down by death rate and Poisson match arrival rate in their model.) I just fix it.
  - ▶ Four types with jobs: Low skill with good job (zero rent), low skill with bad job, high skill with good job, high skill with bad job. I just fix the fraction of each.
  - ▶ I fix the rent associated with a bad job.
- ▶ These assumptions make finding the optimal affine tax pretty easy.
- ▶ Nests model with no bad jobs by setting the fraction of those with bad jobs equal to zero.

# Optimal Tax Problem

$$\max_{b, \tau, c_i, y_i} \pi_0 (u(b)) + \sum_{i \in \{lg, lb, hg, hb\}} \pi_i \left( u(c_i) - v\left(\frac{y_i}{\theta_i}\right) \right)$$

subject to

$$u'(c_i)\theta_i(1 - \tau) = v'\left(\frac{y_i}{\theta_i}\right)$$

$$c_i = b + (1 - \tau)y_i - \text{rent}_i$$

$$b = (\pi_{lb} + \pi_{hb})\text{rent}_b + \tau \sum_i \pi_i y_i.$$

# Optimal Tax Problem

$$\max_{b, \tau, c_i, y_i} \pi_0 (u(b)) + \sum_{i \in \{lg, lb, hg, hb\}} \pi_i \left( u(c_i) - v\left(\frac{y_i}{\theta_i}\right) \right)$$

subject to

$$u'(c_i)\theta_i(1 - \tau) = v'\left(\frac{y_i}{\theta_i}\right)$$

$$c_i = b + (1 - \tau)y_i - rent_i$$

$$b = (\pi_{lb} + \pi_{hb})rent_b + \tau \sum_i \pi_i y_i.$$

- ▶ Tax land rental income is assumed here, and in the paper, to be 100%.
- ▶ If  $(\pi_{lb} + \pi_{hb}) = 0$ , then government revenue from land taxation equals zero.

# Optimal Tax Problem

- ▶ Put in numbers from nowhere and compute.
- ▶  $\pi_0 = .1$ ,  $\pi_i = .225$  for  $i \in \{lg, lb, hg, hb\}$ .
- ▶  $u(c) = .5\sqrt{c}$ .  $v(\frac{y}{\theta}) = .1(\frac{y}{\theta})^2$ .
- ▶  $rent = .1$ ,  $\theta_\ell = 1$ ,  $\theta_h = 2$ .
  
- ▶ With these parameters, I get  $\tau = .21$ .

# Optimal Tax Problem

- ▶ Change parameters.
- ▶  $\pi_0 = .1$ ,  $\pi_{lg} = \pi_{hg} = .45$ ,  $\pi_{lb} = \pi_{hb} = 0$ .
- ▶ (No one has a bad job, ie: No one pays rent.)
- ▶  $u(c) = .5\sqrt{c}$ .  $v(\frac{y}{\theta}) = .1(\frac{y}{\theta})^2$ .
- ▶  $rent = .1$ ,  $\theta_\ell = 1$ ,  $\theta_h = 2$ .
  
- ▶ Now, when I've gotten rid of this extra source of risk, (having to pay rent or not), I get  $\tau = .22$ , or linear taxes went **up**.
- ▶ This is same as in their paper, but with no general equilibrium effects.
- ▶ Again, I would have thought less risk would imply less redistribution and thus a lower, not higher, tax rate.

## What's going on?

- ▶ My guess:
- ▶ The only government expenditure is  $b$  (the intercept term in the affine tax schedule).

$$b = (\pi_{lb} + \pi_{hb})rent_b + \tau \sum_i \pi_i y_i.$$

- ▶ With bad jobs, two sources of revenue: linear tax on output, and 100% tax on rent.
- ▶ Without bad jobs, only one source of revenue, the linear tax on output.
- ▶ May not be surprising that when the 100% tax on revenue not there, you want a higher linear tax on output.

# Conclusion

- ▶ Very nice model.
- ▶ Job ladder model important way of getting at an empirically relevant real-world thing.
- ▶ Might need to do something about the 100% land tax.